

Size-dependent effects in the electron dynamics of metal clusters

Ricardo Díez Muiño
Unidad de Física de Materiales
Centro Mixto CSIC-UPV/EHU
San Sebastián

*ASEVA workshops 2006
WS-19: Physical and Chemical properties of Nanoclusters
Avila (Spain), September 25-27 2006*

 **physics in San Sebastián**



Donostia International
Physics Center
DIPC



Departamento de
Física de Materiales
UPV/EHU



Unidad de Física
de Materiales UFM
CSIC



 **contributors to this work**



Marina Quijada
PhD student UFM
San Sebastián (Spain)

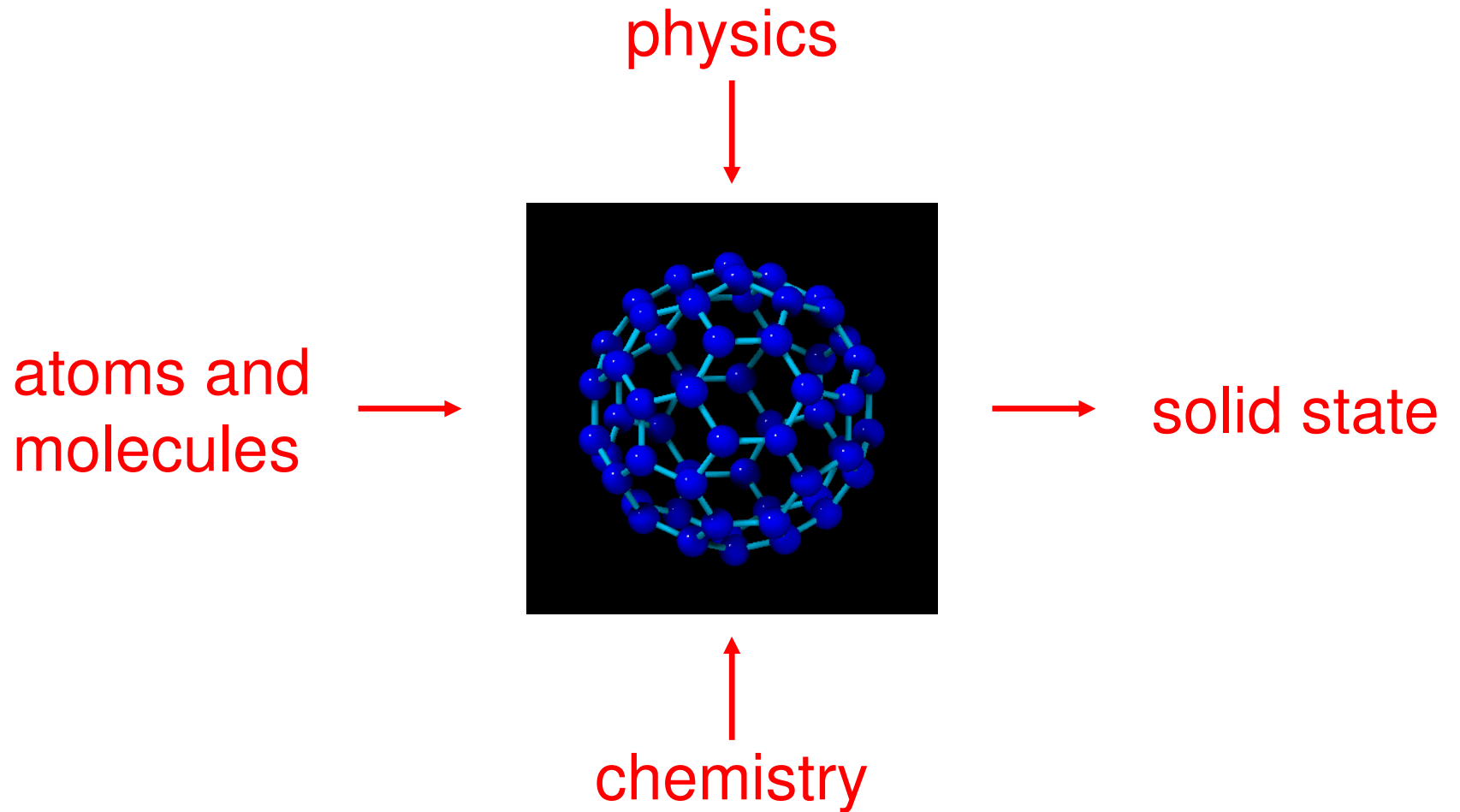


Andrei Borisov
LCAM - U. Paris-Sud
Orsay (France)

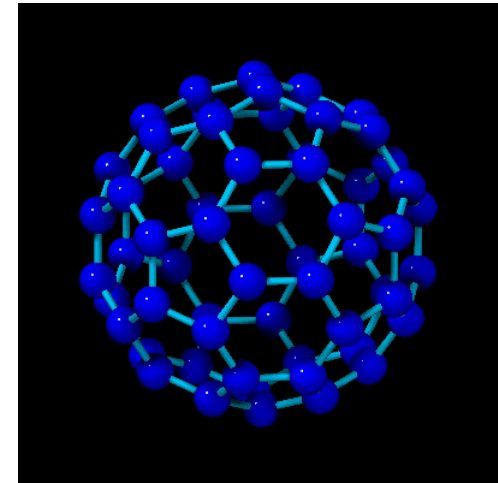
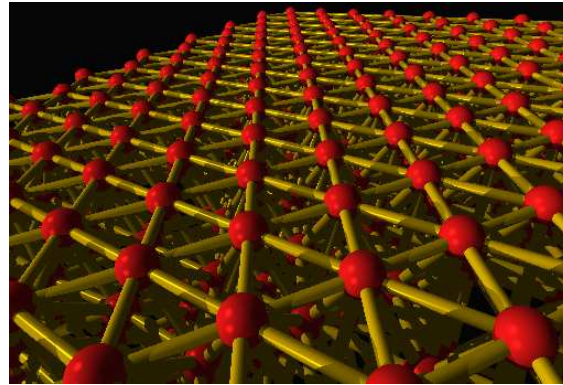


Pedro M. Echenique
UPV/EHU and DIPC
San Sebastián (Spain)

 **clusters as crossroads**



➔ clusters vs. bulk

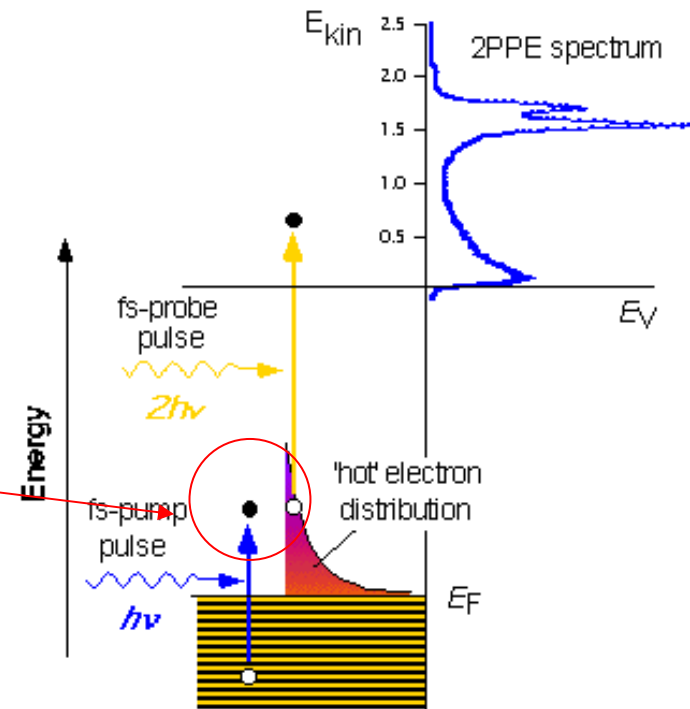


	metal single crystals	metal clusters
geometric structure	simple	complex
electronic structure	electron bands	discrete spectrum
chemical properties	fixed	tunable
optical properties	continous behavior	Mie: resonance behavior

➔ **lifetime of electronic excitations:
2PPE pump-probe experiments**

a first (pump) laser pulse
populates an unoccupied state
and a second (probe) laser pulse
photoemits the electron.

lifetime of
the excitation



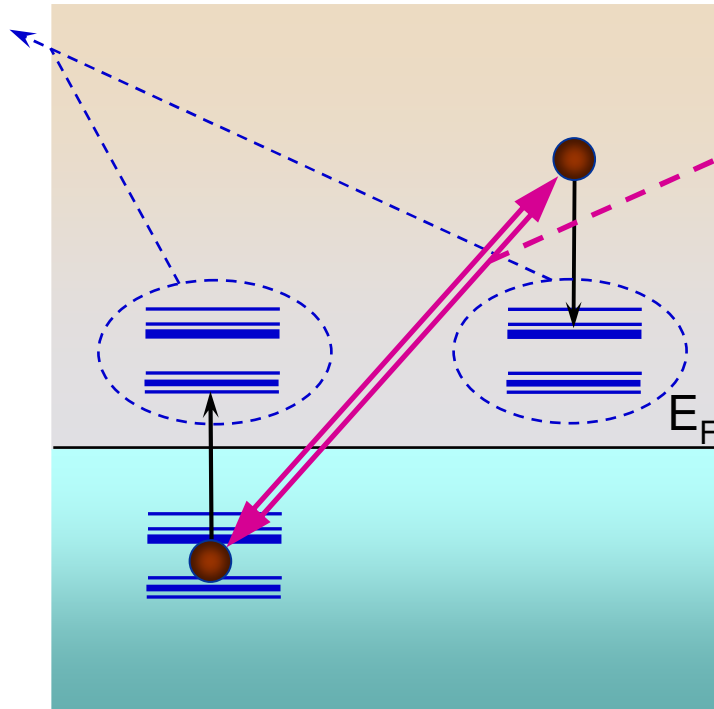
two main channels compete in electron relaxation:

- electron-electron scattering
- electron-phonon interaction

**competition between them determines photochemical activity, for instance
... but also energy transfer, electron transfer across interfaces, etc.**

decay of excitations in a FEG: density of states vs. screening

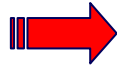
density of states
↓
more DOS
↓
more phase space available
↓
more probability for the process
↓
shorter lifetimes



screening
↓
more DOS
↓
more screening
↓
weaker interaction
↓
longer lifetimes

Free electrons
Quinn (1962)

$$\tau \approx \frac{263 r_s^{-5/2}}{(E-E_F)^2} \propto \frac{n^{5/6}}{(E-E_F)^2}$$



questions to solve:

**how does the lifetime of electronic excitations
change when moving from infinite to
finite nano-sized systems?**

**which is the dependence with size
of the electronic excitation lifetimes?**

➔ **lifetimes in clusters vs. lifetimes in solids:
DOS effects**

**discretization of
levels**

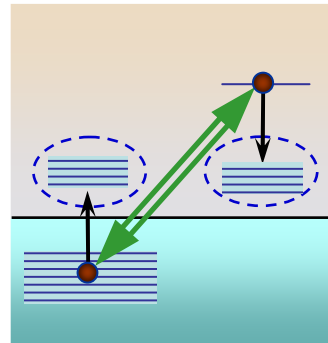


less phase space
available

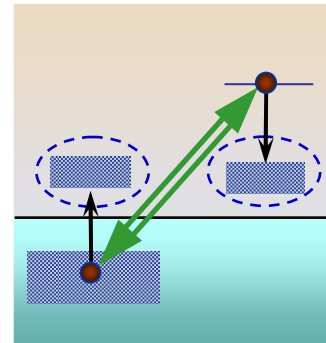


longer lifetimes

clusters



FEG



continuum spectrum



more phase space
available



shorter lifetimes

$$\tau_{\text{cluster}} > \tau_{\text{FEG}} ?$$

lifetimes in clusters vs. lifetimes in solids: screening effects

surface effects
and less electron
mobility

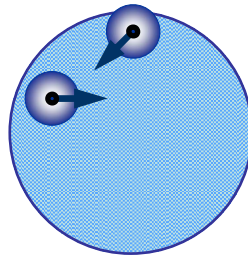


less screening

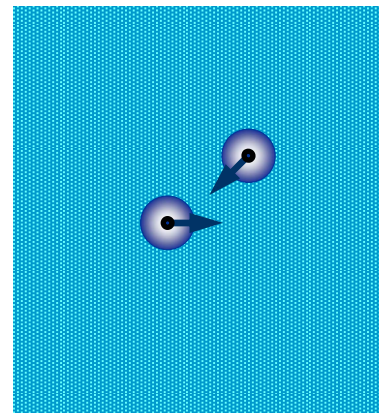


shorter lifetimes

clusters



FEG



no surface,
free electrons



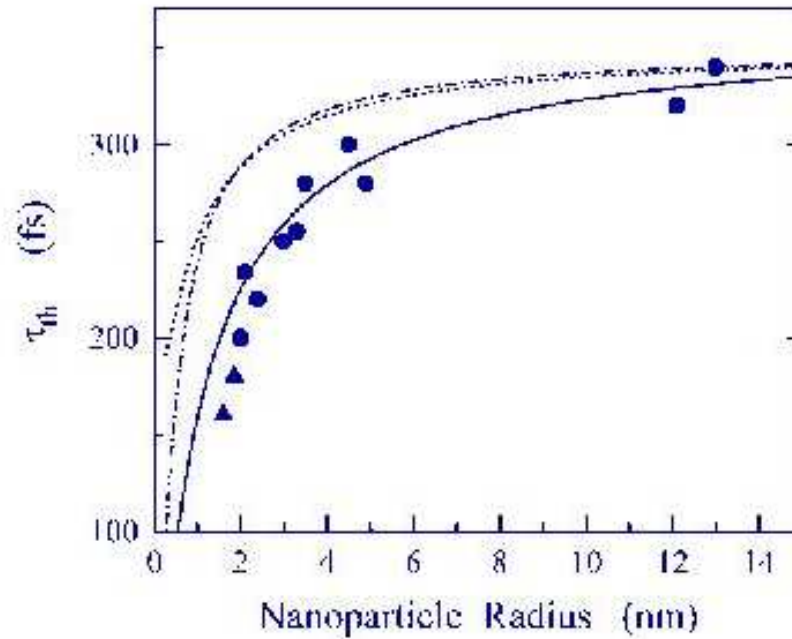
more screening



longer lifetimes

$$\tau_{\text{cluster}} < \tau_{\text{FEG}} ?$$

➔ experimental measurements of size-dependent electron dynamics



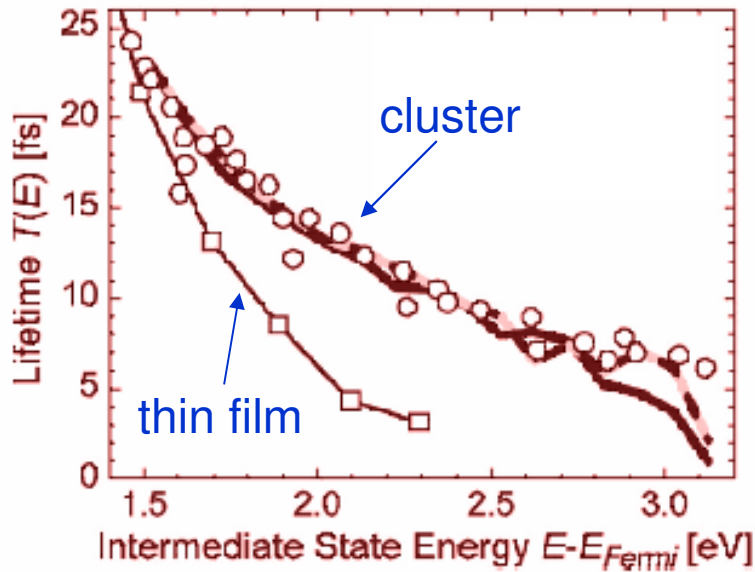
Ag nanoparticles

Voisin *et al.*,
Size-dependent electron-electron
interactions in metal nanoparticles
PRL 85, 2200 (2000)

A sharp increase of the electron energy exchange rate is demonstrated for nanoparticles smaller than 5 nm. ... due to surface induced reduction of the Coulomb interaction screening.

$$\tau_{cl} < \tau_{bulk}$$

➔ experimental measurements of size-dependent electron dynamics



Ag 2nm nanoparticles

Merschdorf *et al.*,
Collective and single-particle dynamics
in time-resolved two-photon photoemission
PRB 70, 193401 (2004)

*Experiments performed with TR 2PPES
on bulk Ag yield
significantly lower lifetimes
(as compared to clusters).*

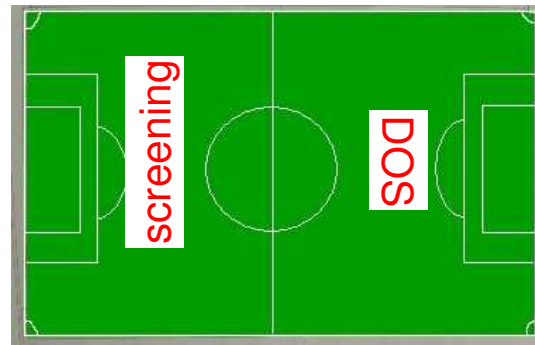
$$\tau_{cl} > \tau_{bulk}$$

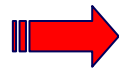
➔ lifetimes in clusters vs. lifetimes in solids

screening arguments: $\tau_{\text{cluster}} < \tau_{\text{FEG}} ?$

DOS arguments: $\tau_{\text{cluster}} > \tau_{\text{FEG}} ?$

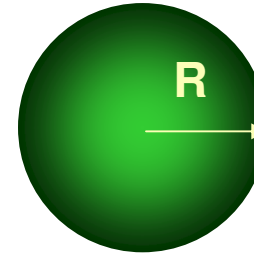
$\tau_{\text{cluster}} \lesseqgtr \tau_{\text{FEG}} ?$





1st step: DFT calculation of a jellium cluster

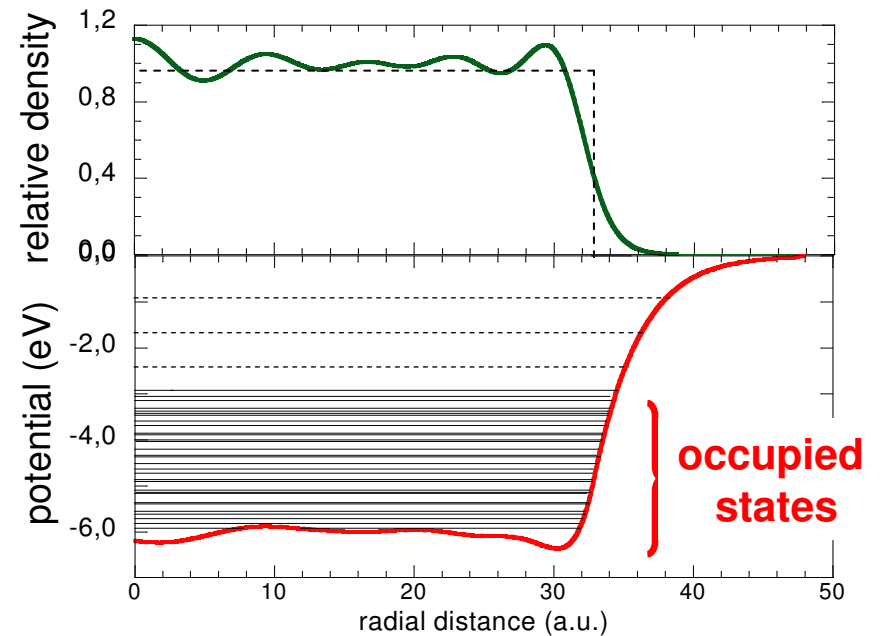
cluster is described in the jellium model (a background of constant positive charge)



Kohn-Sham equations
solved self-consistently

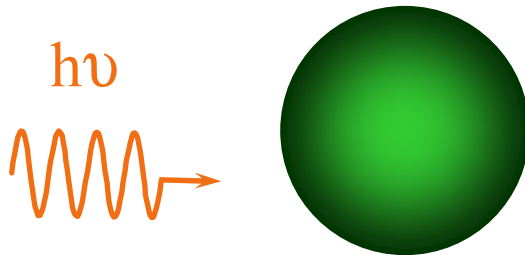
$$\left\{ -\frac{1}{2} \nabla^2 + v_{\text{eff}}(\mathbf{r}) \right\} \varphi_i(\mathbf{r}) = \varepsilon_i \varphi_i(\mathbf{r})$$

$$v_{\text{eff}}(\mathbf{r}) = v_{\text{jellium}}(\mathbf{r}) + v_{\text{Hartree}}(\mathbf{r}) + v_{\text{xc}}(\mathbf{r})$$

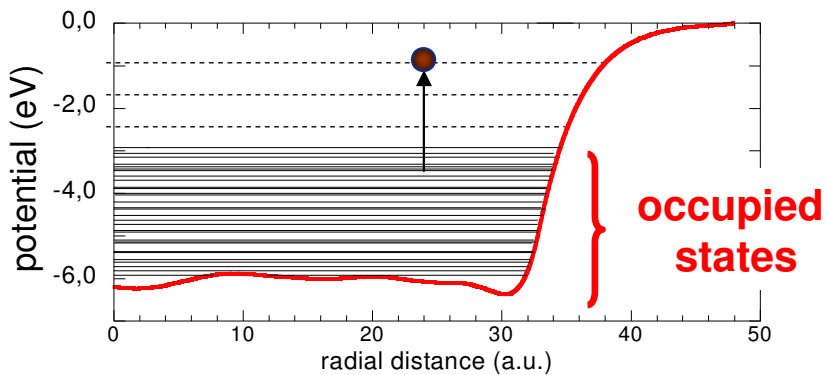


lifetimes of electronic excitations in metal clusters

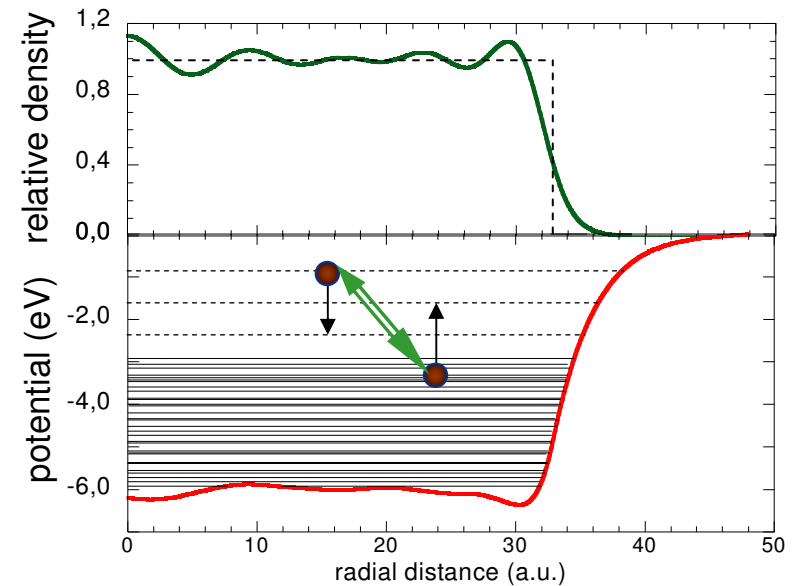
metallic clusters in excited electronic states



(excited by incident laser light, for instance)



decay of excitation through electron-electron interaction



➔ **2nd step: calculation of the linear response function $\chi(\mathbf{r},\mathbf{r}',\omega)$ and of the screened interaction $W(\mathbf{r},\mathbf{r}',\omega)$**

2a- independent-particle response function $\chi_0(\mathbf{r},\mathbf{r}',\omega)$

$$\chi_0(\mathbf{r},\mathbf{r}',\omega) = \sum_{\varphi_2 \in \text{occ.}} \sum_{\varphi_3 \notin \text{occ.}} \left[\frac{\varphi_2^*(\mathbf{r})\varphi_2(\mathbf{r}')\varphi_3^*(\mathbf{r}')\varphi_3(\mathbf{r})}{\omega + \varepsilon_2 - \varepsilon_3 + i\delta} - \frac{\varphi_2(\mathbf{r})\varphi_2^*(\mathbf{r}')\varphi_3(\mathbf{r}')\varphi_3^*(\mathbf{r})}{\omega - \varepsilon_2 + \varepsilon_3 + i\delta} \right]$$

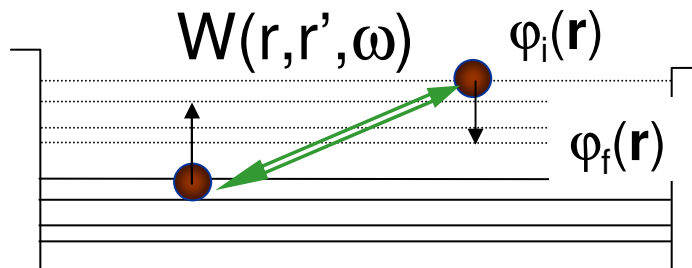
2b- self-consistent calculation of $\chi(\mathbf{r},\mathbf{r}',\omega)$ in real space (RPA)

$$\chi(\mathbf{r},\mathbf{r}',\omega) = \chi_0(\mathbf{r},\mathbf{r}',\omega) + \int d\mathbf{r}_1 d\mathbf{r}_2 \chi_0(\mathbf{r},\mathbf{r}_1,\omega) \left[\frac{1}{|\mathbf{r}_1 - \mathbf{r}_2|} \right] \chi(\mathbf{r}_2,\mathbf{r}',\omega)$$

2c- calculation of the screened Coulomb interaction $W(\mathbf{r},\mathbf{r}',\omega)$

$$W(\mathbf{r},\mathbf{r}',\omega) = \frac{1}{|\mathbf{r} - \mathbf{r}'|} + \int d\mathbf{r}_1 d\mathbf{r}_2 \left[\frac{1}{|\mathbf{r} - \mathbf{r}_1|} \right] \chi(\mathbf{r}_1,\mathbf{r}_2,\omega) \left[\frac{1}{|\mathbf{r}_2 - \mathbf{r}'|} \right]$$

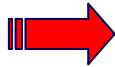
➔ **3rd step: calculation of the imaginary part of the self-energy
GW approximation**



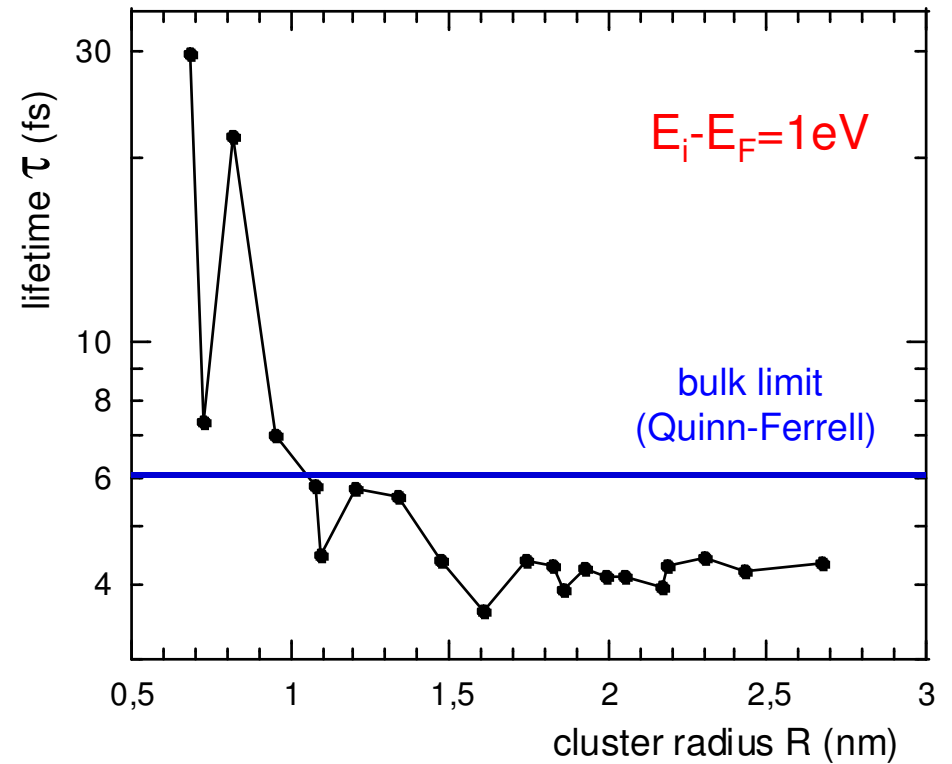
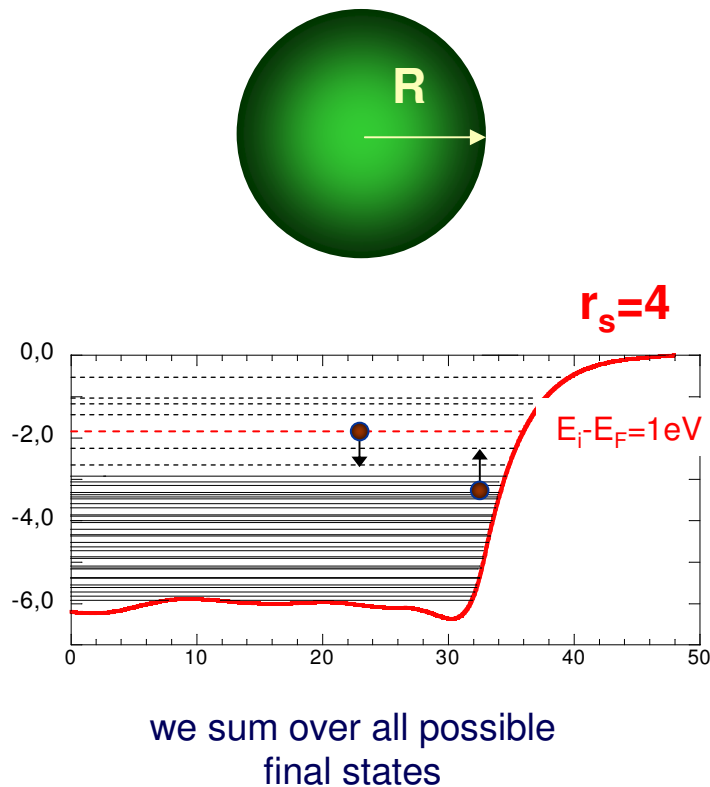
$\varphi_i(\mathbf{r})$ is a KS unoccupied wavefunction that represents the initial state in the decay
 $\varphi_f(\mathbf{r})$ is a KS unoccupied wavefunction that represents the final state in the decay

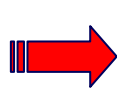
calculation of the decay rate $\Gamma = \tau^{-1}$

$$\Gamma_i = -2 \sum_{f \notin occ.} \int d\mathbf{r} d\mathbf{r}' \varphi_i^*(\mathbf{r}) \varphi_f^*(\mathbf{r}') \text{Im} W(\mathbf{r}, \mathbf{r}', \omega) \varphi_i(\mathbf{r}') \varphi_f(\mathbf{r})$$

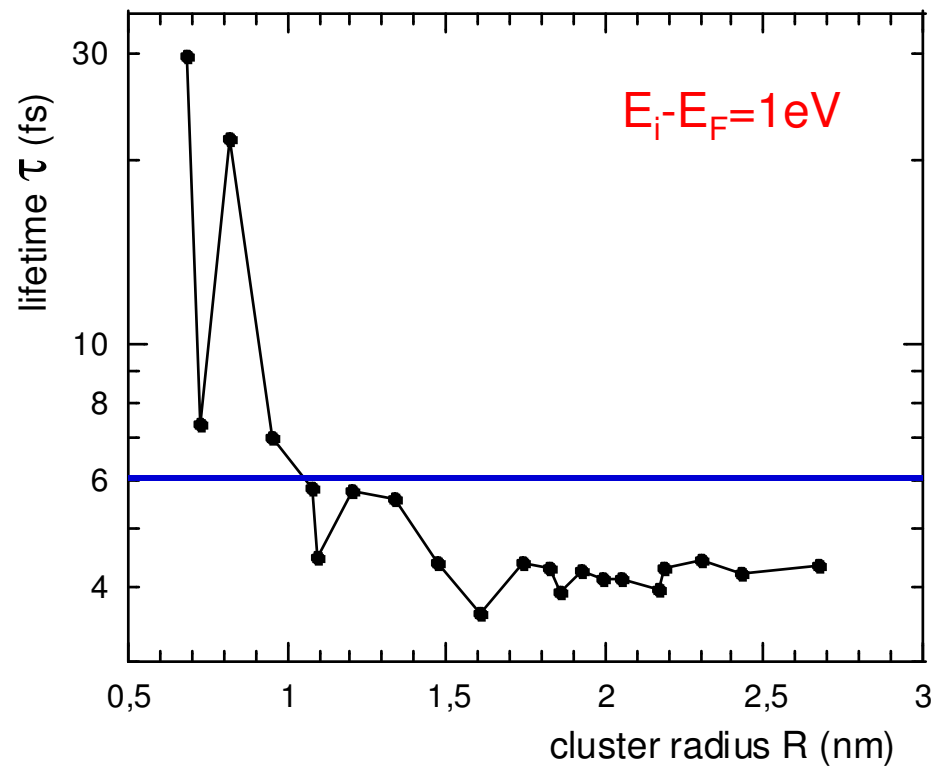


size-dependence of the decay rate for electrons excited ~ 1 eV above the Fermi level





size-dependence of the decay rate for electrons excited ~ 1 eV above the Fermi level



electron lifetimes in clusters range between 3 and 30 fs for $E \sim 1$ eV

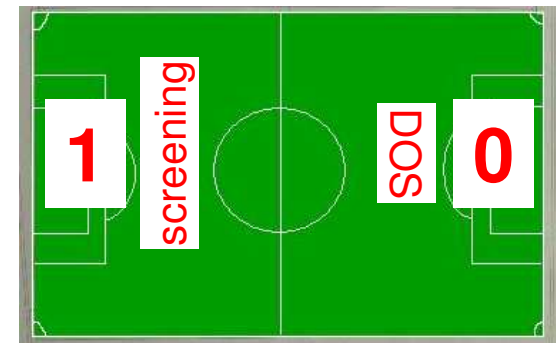


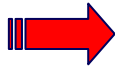
order of magnitude is similar in a FEG



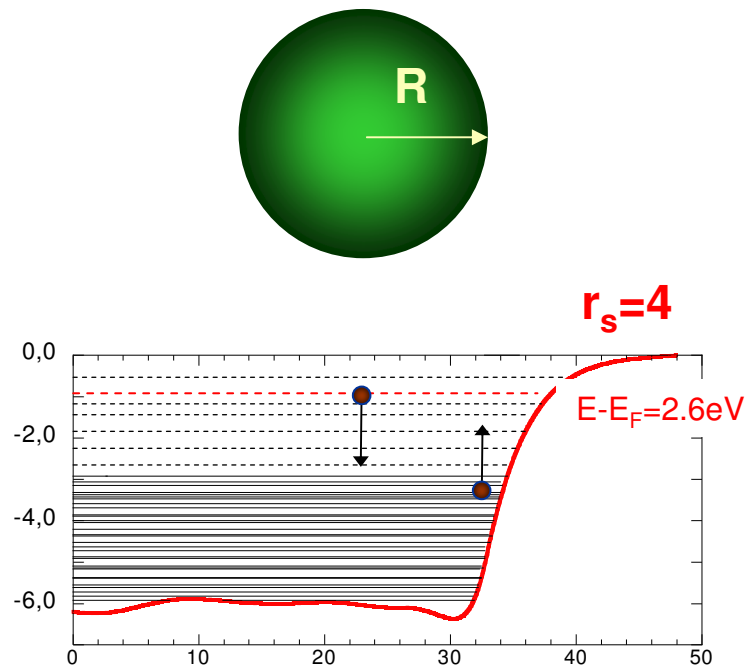
oscillations due to the discretization of levels

$$\tau_{\text{cluster}} < \tau_{\text{FEG}}!$$

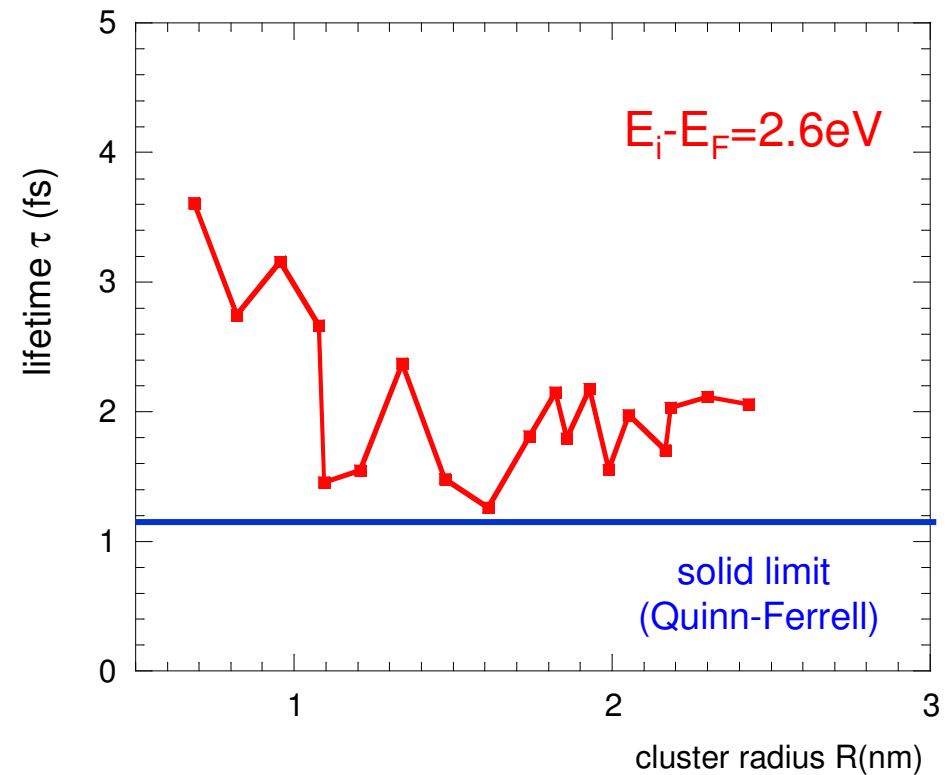


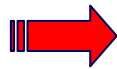


size-dependence of the decay rate for electrons excited ~ 2.6 eV above the Fermi level

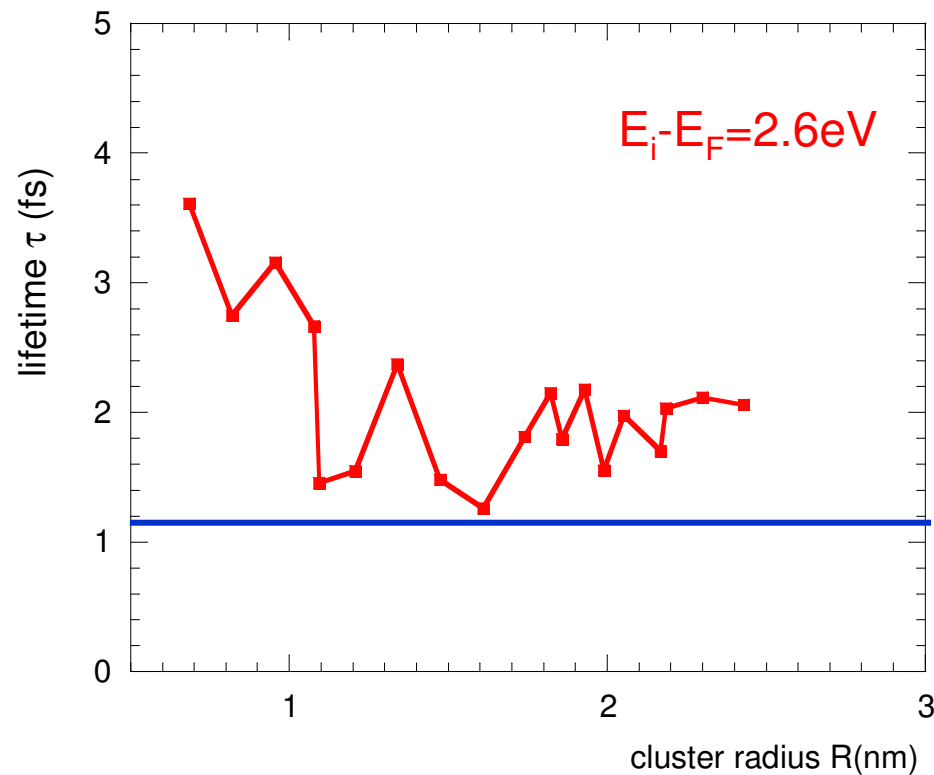


we sum over all possible final states



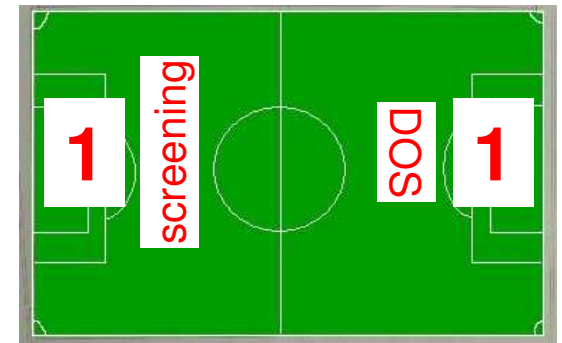


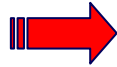
size-dependence of the decay rate for electrons excited ~ 2.6 eV above the Fermi level



Electron lifetimes in clusters range are ~ 2 fs for $E \sim 2.6$ eV (slightly longer than solids)

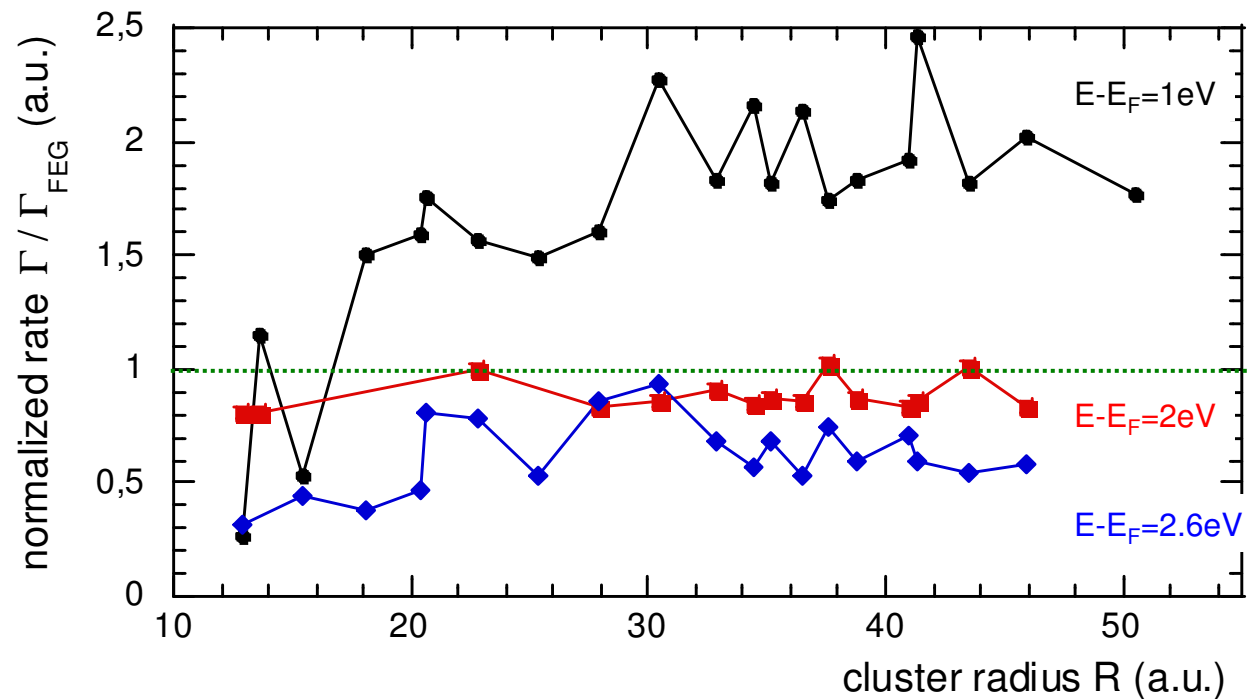
$$\tau_{\text{cluster}} > \tau_{\text{FEG}}!$$



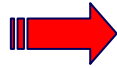


size-dependence of the decay rate for electrons

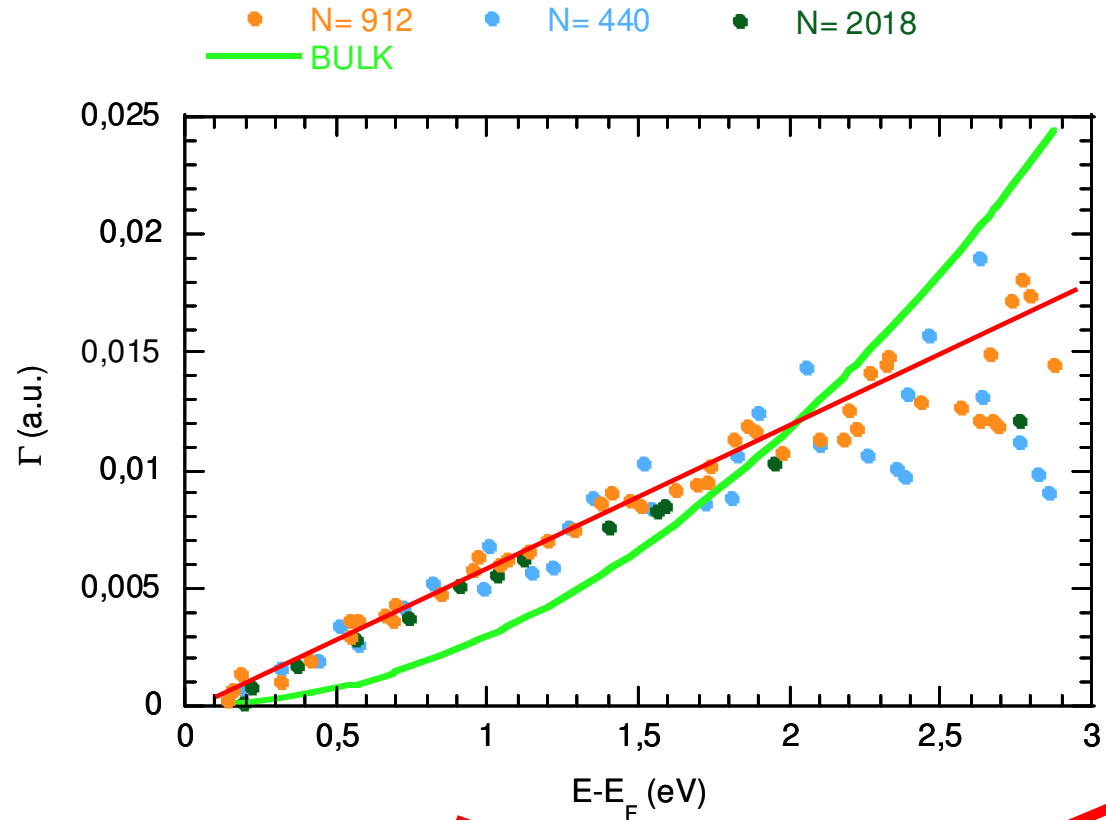
decay rate Γ normalized to the solid (FEG) value



$$\tau_{\text{cluster}} \lesseqgtr \tau_{\text{FEG}} ?$$

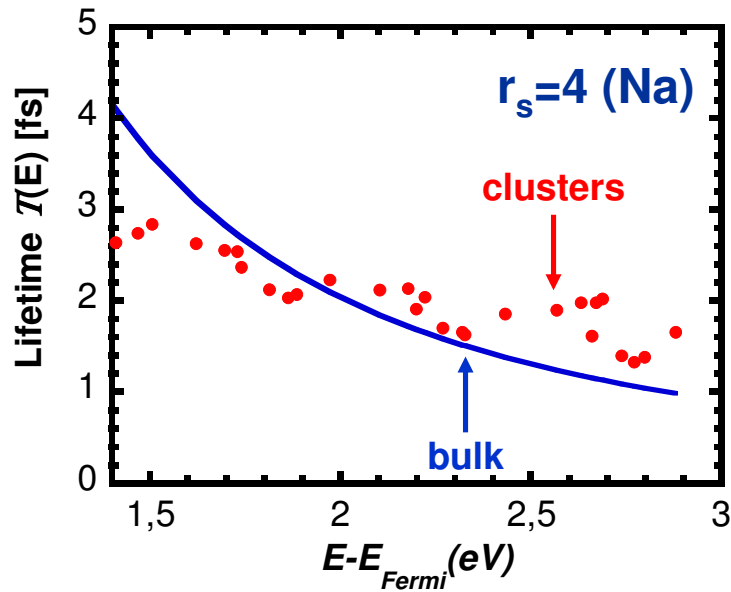


initial energy dependence of the decay rate

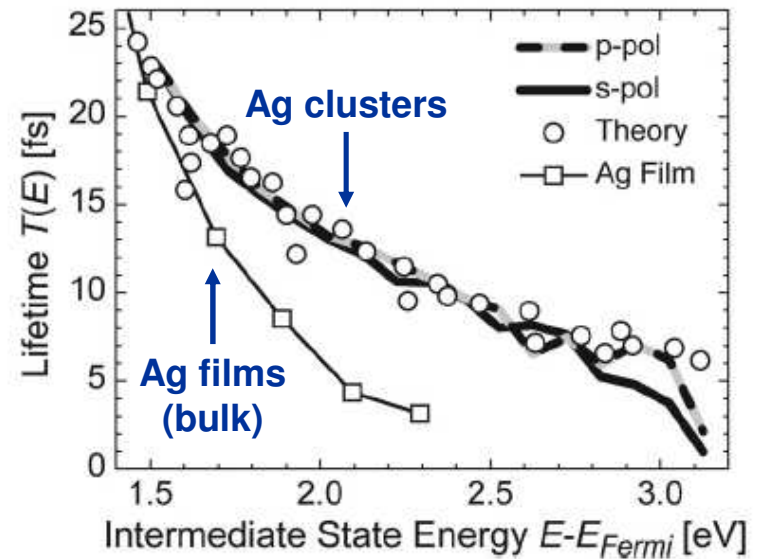


free electrons: $\tau \approx \frac{263 r_s^{-5/2}}{(E-E_F)^2} \propto \frac{n^{5/6}}{(E-E_F)^2}$

→ comparison of lifetimes in solids and nanosized clusters



Theoretical calculation
for (gas-phase) Na clusters
of ~ 4nm diameter



Experimental measurements
for (supported) Ag clusters
of ~ 2.2nm diameter
Merschdorf *et al.*,
PRB **70**, 193401 (2004)

electron lifetimes in metal nanoparticles: conclusions



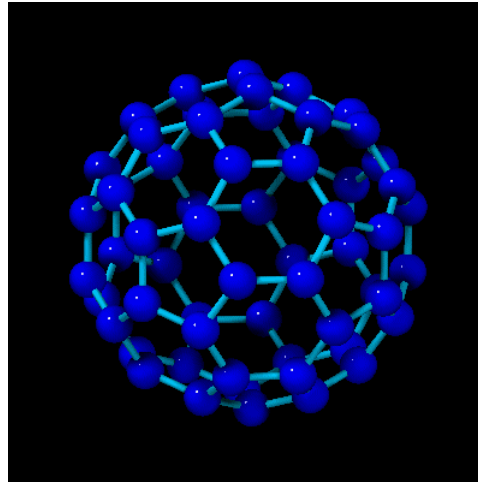
Electron lifetimes in metal clusters are of the order of few femtoseconds (not far from those in solids), for sufficiently large (nm) clusters



Nevertheless, in this size range, there are apparent differences with respect to the free-electron gas: lifetimes can be either larger or shorter depending on the excitation energy



There is not a clear winner in the screening versus DOS competition: the free-electron gas dependence $\tau \sim 1/(E-E_F)^2$ is broken!



thank you for your attention



ASEVA workshops 2006
WS-19: Physical and Chemical properties of Nanoclusters
Avila (Spain), September 25-27 2006